

# Reteaching 6-1

## Scientific Notation

To write a number such as 67,000 in *scientific notation*, move the decimal point to form a number between 1 and 10. The number of places moved shows which power of 10 to use.

- Write 67,000 in scientific notation.

6.7 is between 1 and 10. So, move the decimal point in 67,000 to the left 4 places and multiply by  $10^4$ .

$$67,000 = 6.7 \times 10^4$$

To write scientific notation in *standard form*, look at the exponent. The exponent shows the number of places and the direction to move the decimal point.

- Write  $8.5 \times 10^5$  in standard form.

The exponent is positive 5, so move the decimal point 5 places to the right.

$$8.5 \times 10^5 = 850,000$$

### Write each number in scientific notation.

1. 6,500  
\_\_\_\_\_

2. 65,000  
\_\_\_\_\_

3. 6,520  
\_\_\_\_\_

4. 345  
\_\_\_\_\_

5. 29,100  
\_\_\_\_\_

6. 93,000,000  
\_\_\_\_\_

7. 200  
\_\_\_\_\_

8. 2,300  
\_\_\_\_\_

9. 23,000  
\_\_\_\_\_

### Write each number in standard form.

10.  $4 \times 10^4$  \_\_\_\_\_

11.  $4 \times 10^5$  \_\_\_\_\_

12.  $3.6 \times 10^3$  \_\_\_\_\_

13.  $4.85 \times 10^4$  \_\_\_\_\_

14.  $4.05 \times 10^2$  \_\_\_\_\_

15.  $7.1 \times 10^5$  \_\_\_\_\_

16.  $4 \times 10^2$  \_\_\_\_\_

17.  $1.3 \times 10^2$  \_\_\_\_\_

18.  $7 \times 10^1$  \_\_\_\_\_

19.  $1.81 \times 10^3$  \_\_\_\_\_

20. Jupiter orbits at an average of  $7.783 \times 10^8$  kilometers from the Sun. \_\_\_\_\_

### Which number is greater?

21.  $5 \times 10^2$  or  $2 \times 10^5$  \_\_\_\_\_

22.  $2.1 \times 10^3$  or  $2.1 \times 10^6$  \_\_\_\_\_

23.  $6 \times 10^{10}$  or  $3 \times 10^9$  \_\_\_\_\_

24.  $3.6 \times 10^1$  or  $3.6 \times 10^3$  \_\_\_\_\_

# Reteaching 6-2

## Exponents and Multiplication

- To multiply numbers or variables with the same base, add the exponents.

$$\begin{aligned} \text{Simplify } 3^2 \cdot 3^4 \\ 3^2 \cdot 3^4 &= 3^{(2+4)} \\ &= 3^6 \end{aligned}$$

$$\begin{aligned} \text{Simplify } n^3 \cdot n^4 \\ n^3 \cdot n^4 &= n^{(3+4)} \\ &= n^7 \end{aligned}$$

$$\begin{aligned} \text{Simplify } (-4)^3 \cdot (-4)^5 \\ (-4)^3 \cdot (-4)^5 &= (-4)^{(3+5)} \\ &= (-4)^8 \end{aligned}$$

- You can also simplify expressions with exponents.

$$\begin{aligned} 6x^2 \cdot -2x^5 &= 6 \cdot -2 \cdot x^2 \cdot x^5 && \leftarrow \text{Use the Commutative Property of Multiplication} \\ &= -12x^{(2+5)} && \leftarrow \text{Add the exponents.} \\ &= -12x^7 && \leftarrow \text{Simplify.} \end{aligned}$$

Write each expression using a single exponent.

1.  $5^3 \cdot 5^4$

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2.  $a^2 \cdot a^5$

\_\_\_\_\_

3.  $(-8)^4 \cdot (-8)^5$

\_\_\_\_\_

4.  $n^6 \cdot n^2$

\_\_\_\_\_

5.  $m^3 \cdot m^6$

\_\_\_\_\_

6.  $(-7)^4 \cdot (-7)^2$

\_\_\_\_\_

7.  $(-3)^2 \cdot (-3)^2$

\_\_\_\_\_

8.  $2^5 \cdot 2^2$

\_\_\_\_\_

9.  $c^5 \cdot c^3$

\_\_\_\_\_

Find each product. Write the answer in scientific notation.

10.  $2x^3 \cdot x^2$

\_\_\_\_\_

11.  $-4x^3 \cdot 2x^4$

\_\_\_\_\_

12.  $3a^3 \cdot a$

\_\_\_\_\_

13.  $-x^2 \cdot 2x^3$

\_\_\_\_\_

14.  $-5m^2 \cdot -2m^4$

\_\_\_\_\_

15.  $x^8 \cdot x^4$

\_\_\_\_\_

# Reteaching 6-3

## Multiplying with Scientific Notation

- To multiply numbers in scientific notation.

Find the product  $(5 \times 10^4)(7 \times 10^5)$ . Write the result in scientific notation.

$$(5 \times 10^4)(7 \times 10^5)$$

$$(5 \cdot 7)(10^4 \cdot 10^5) \quad \leftarrow \quad \text{Use the Associative and Commutative properties.}$$

$$35 \times (10^4 \cdot 10^5) \quad \leftarrow \quad \text{Multiply 5 and 7.}$$

$$35 \times 10^{4+5} \quad \leftarrow \quad \text{Add the exponents for the powers of 10.}$$

$$35 \times 10^9$$

$$3.5 \times 10^1 \times 10^9 \quad \leftarrow \quad \text{Write 35 in scientific notation.}$$

$$3.5 \times 10^{10} \quad \leftarrow \quad \text{Add the exponents.}$$

**Find each product. Write the answer in scientific notation.**

1.  $(3 \times 10^4)(5 \times 10^3)$

2.  $(2 \times 10^3)(7 \times 10^6)$

\_\_\_\_\_

\_\_\_\_\_

3.  $(8 \times 10^2)(5 \times 10^2)$

4.  $(9 \times 10^4)(7 \times 10^4)$

\_\_\_\_\_

\_\_\_\_\_

5.  $(4 \times 10^2)(7 \times 10^5)$

6.  $(8 \times 10^3)(4 \times 10^5)$

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**Reteaching 6-4****Exponents and Division**

To divide powers with the same base, subtract exponents.

$$\begin{aligned}\frac{8^6}{8^4} &= 8^{6-4} & \frac{a^5}{a^3} &= a^{5-3} \\ &= 8^2 & &= a^2 \\ &= 64 & &\end{aligned}$$

- For any nonzero number  $a$ ,  $a^0 = 1$ .

$$3^0 = 1 \quad (-6)^0 = 1 \quad 4t^0 = 4(1) = 4$$

- For any nonzero number  $a$  and any integer  $n$ ,  $a^{-n} = \frac{1}{a^n}$ .

$$\begin{aligned}2^{-4} &= \frac{1}{2^4} & 3c^{-2} &= \frac{3}{c^2} & \frac{5^3}{5^6} &= 5^{3-6} & \frac{10z^3}{5z} &= 2z^{3-1} \\ &= \frac{1}{16} & & & &= 5^{-3} & &= 2z^2 \\ & & & & &= \frac{1}{5^3} & & \\ & & & & &= \frac{1}{125} & &\end{aligned}$$

**Simplify each expression.**

$$1. \frac{6^5}{6^3} = \underline{\hspace{2cm}} \quad 2. (-4)^5 \div (-4)^3 = \underline{\hspace{2cm}} \quad 3. (-3)^{-2} = \underline{\hspace{2cm}}$$

$$4. \frac{2^5}{2^7} = \underline{\hspace{2cm}} \quad 5. (-8)^0 = \underline{\hspace{2cm}} \quad 6. \frac{5^0}{5^2} = \underline{\hspace{2cm}}$$

$$7. \frac{(-6)^4}{(-6)^6} = \underline{\hspace{2cm}} \quad 8. 7^3 \div 7^5 = \underline{\hspace{2cm}} \quad 9. 9^8 \div 9^{10} = \underline{\hspace{2cm}}$$

**Simplify each expression. Write your answer using only positive exponents.**

$$10. w^8 \div w^3 = \underline{\hspace{2cm}} \quad 11. x^6 \div x^1 = \underline{\hspace{2cm}} \quad 12. \frac{d^7}{d^3} = \underline{\hspace{2cm}}$$

$$13. \frac{w^2}{w^6} = \underline{\hspace{2cm}} \quad 14. 4c^5 \div c^8 = \underline{\hspace{2cm}} \quad 15. \frac{8x^2}{4x^5} = \underline{\hspace{2cm}}$$

$$16. 8a^4 \div 2a^2 = \underline{\hspace{2cm}} \quad 17. 6w^2 \div 2w^5 = \underline{\hspace{2cm}} \quad 18. \frac{6x^6}{3x^9} = \underline{\hspace{2cm}}$$

# Reteaching 6-5

## Dividing with Scientific Notation

You can separate the coefficients and powers of ten to divide numbers in scientific notation.

$$\begin{aligned}
 (8.4 \times 10^6) \div (2.5 \times 10^4) &= \frac{8.4 \times 10^6}{2.5 \times 10^4} && \leftarrow \text{Write a fraction.} \\
 &= \frac{8.4}{2.5} \times \frac{10^6}{10^4} && \leftarrow \text{Separate the coefficients and the power of ten.} \\
 &\approx 3.4 \times \frac{10^6}{10^4} && \leftarrow \text{Divide the coefficients.} \\
 &\approx 3.4 \times 10^2 && \leftarrow \text{Subtract the exponents.}
 \end{aligned}$$

You can divide numbers in standard form by numbers in scientific notation.

$$\begin{aligned}
 (9.2 \times 10^4) \div 4.8 &= \frac{9.2 \times 10^4}{4.8} && \leftarrow \text{Write a fraction.} \\
 &= \frac{9.2}{4.8} \times 10^4 && \leftarrow \text{Write as a product of} \\
 &&& \text{quotients and a power} \\
 &&& \text{of ten.} \\
 &\approx 1.9 \times 10^4 && \leftarrow \text{Divide.}
 \end{aligned}$$

You can divide numbers in scientific notation by numbers in standard form.

$$\begin{aligned}
 6.8 \div (3.9 \times 10^2) &= \frac{6.8}{3.9 \times 10^2} && \leftarrow \text{Write a} \\
 &&& \text{fraction.} \\
 &\approx \frac{6.8}{3.9} \times \frac{1}{10^2} && \leftarrow \text{Write as a} \\
 &&& \text{product of} \\
 &&& \text{quotients} \\
 &&& \text{and a power} \\
 &&& \text{of ten.} \\
 &\approx 1.7 \times 10^{-2}
 \end{aligned}$$

**Divide. Write each quotient in scientific notation. Round answers to the nearest tenth.**

1.  $\frac{6.4 \times 10^5}{1.8 \times 10^3}$

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2.  $\frac{7.4 \times 10^4}{3.3}$

\_\_\_\_\_

3.  $\frac{8}{2.6 \times 10^2}$

\_\_\_\_\_

4.  $\frac{9.2 \times 10^4}{5.9 \times 10^2}$

\_\_\_\_\_

5.  $\frac{6.5 \times 10^8}{8.9}$

\_\_\_\_\_

6.  $\frac{12.2}{6.3 \times 10^4}$

\_\_\_\_\_

7.  $\frac{5.4 \times 10^2}{0.5}$

\_\_\_\_\_

8.  $\frac{3.4 \times 10^8}{1.2 \times 10^6}$

\_\_\_\_\_